## SPH4U 7.1 Properties of Electric Charge

## 1. Electric charge

| Law of electric charges: | $\leftrightarrow+\quad \oplus \rightarrow \begin{aligned} & \text { Like } \\ & \text { Lharges } \\ & \text { repel. }\end{aligned}$ |
| :---: | :---: |
| Law of conservation of charge: | $\oplus \rightarrow \leftarrow \odot \begin{gathered}\text { Unlike } \\ \text { charges } \\ \text { attract. }\end{gathered}$ |
| coulomb |  |

## 2. Conductors and insulators

| Conductor: |  |
| :---: | :---: |
| Insulator: |  |
| liquids and gases |  |
| charging an insulator |  |
| charging a conductor |  |

## 3. Charging objects

| By friction: | acetate | weak hold on |
| :---: | :---: | :---: |
|  | $\substack{\text { glass } \\ \text { wool } \\ \text { catur human hair }}$ <br> cal |  |
|  | cat utur, human haircalcum, lead |  |
|  |  | increasingtendency |
|  |  |  |
|  | $\begin{aligned} & \text { duturn } \\ & \text { cotron } \\ & \text { paraffin wax } \end{aligned}$ ebonte | to gain electrons |
| electrostatic series | polyethylene (plastic) carbon, copper, nickel sulur |  |
|  |  |  |
|  | sulfur <br> platinum, gold | strong hold on |

By induced
charge
separation:


## 4. Grounding



Charging by induction:


## SPH4U 7.2 Coulomb's Law

## 1. Electric force

Electric force:

Coulomb's law:
Coulomb's
constant
direction


Superposition principal:

An early model of the hydrogen atom had the electron revolving around the proton, like the Earth revolves around the Sun.
a. The distance between the electron and the proton in a hydrogen atom is $5.3 \times 10^{-11}$ m , the charge of each is $1.6 \times 10^{-19} \mathrm{C}$, the mass of the electron is $9.11 \times 10^{-31} \mathrm{~kg}$, and the mass of the proton is $1.67 \times 10^{-27} \mathrm{~kg}$. Calculate the ratio of the electric force $\mathrm{F}_{\mathrm{E}}$ to the gravitational force Fg .
b. Determine the accelerations of the electron caused by both the electric force and the gravitational force.

Two charges, $\mathrm{q}_{1}=-2.00 \times 10^{-6} \mathrm{C}$ and $\mathrm{q}_{2}=-1.80 \times 10^{-5} \mathrm{C}$ are separated by a distance, L , of 4.00 m . A third charge, $\mathrm{q}_{3}=+1.50 \times 10^{-6} \mathrm{C}$, is placed somewhere between $\mathrm{q}_{1}$ and $\mathrm{q}_{2}$. The net force exerted on $q_{3}$ by the other two charges is zero. Determine the location of $q_{3}$.


Two point particles have equal but opposite charges of $+q_{1}$ and $-q_{1}$. The particles are arranged as shown. Suppose a charge $\mathrm{q}_{2}$ is placed on the x -axis as shown. $\mathrm{q}_{1}=$ $5.0 \times 10^{-6} \mathrm{C}, \mathrm{q}_{2}=1.0 \times 10^{-6} \mathrm{C}$, and the distance between $+\mathrm{q}_{1}$ and $-\mathrm{q}_{1}$ is 8.0 m measured vertically along the $y$-axis. Calculate the magnitude and the direction of the net electric force on $\mathrm{q}_{2}$.


## SPH4U 7.3 Electric Fields

## 1. Electric fields



Two point charges are 45 cm apart. The charge on $\mathrm{q}_{1}$ is 3.3 x $10^{-9} \mathrm{C}$, and the charge on $\mathrm{q}_{2}$ is $-1.00 \times 10^{-8} \mathrm{C}$.

a. Calculate the net electric field at point $P, 27 \mathrm{~cm}$ from the positive charge, on the line connecting the charges.
b. A new charge of $+2.0 \times 10^{-12} \mathrm{C}$ is placed at P . Determine the electric force on this new charge.

Two point charges are arranged as shown. $\mathrm{q}_{1}=4.0 \times 10^{-6} \mathrm{C}, \mathrm{q}_{2}=-2.0 \times 10^{-6} \mathrm{C}$, and $\mathrm{r}=$ 3.0 cm . Calculate the magnitude of the electric field at the origin.


## 2. Electric field lines

| Electric field <br> lines: |  |
| :---: | :--- |
| direction |  |
| inverse |  |
| square law |  |



## 3. Electric dipoles

| Electric dipole: |  |
| :---: | :--- |
| field lines |  |
| Two +q charges: |  |
| $+2 q$ and $-q:$ |  |



Uniform electric
field:


## SPH4U 7.4 Potential Difference and Electric Potential

## 1. Electric potential energy

| Electric potential energy: |  |
| :---: | :---: |
| equation | $\vec{F}_{E}$ |
| direction | $\Delta E_{\mathrm{E}}>0$ |

A charged particle moves from rest in a uniform electric field.
a. For a proton, calculate the change in electric potential energy when the magnitude of the electric field is $250 \mathrm{~N} / \mathrm{C}$, the starting position is 2.4 m from the origin, and the final position is 3.9 m from the origin.
b. Calculate the change in electric potential energy for an electron in the same field and with the same displacement.
c. Using the law of conservation of energy, calculate the final speed of the proton in part (a), assuming that the proton starts from rest.
d. Determine the initial speed of the electron in part (b), assuming its final speed has decreased to half of its initial speed.

## 2. Electric potential

| Electric potential: |  |
| :---: | :---: |
| equation | potential difference $=\Delta v$ <br> $\varepsilon=-\Delta v$ |
| Electric potential difference: |  |
| equation |  |
| uniform electric field |  |

The cathode-ray tubes in old televisions use a uniform electric field to accelerate particles.
a. An electron leaves the negative plate of a cathode-ray tube (CRT) toward the positive plate. The electric potential difference between the plates is $1.5 \times 10^{4} \mathrm{~V}$. Using conservation of energy, calculate the final speed of the electron, assuming that it is initially at rest. The mass of an electron is $9.11 \times 10^{-31} \mathrm{~kg}$.
b. The two plates are 15 cm apart. Calculate the magnitude of the electric field.

An electron moves horizontally with a speed of $1.6 \times 10^{6} \mathrm{~m} / \mathrm{s}$ between two horizontal parallel plates. The plates have a length of 12.5 cm . The electric field within the plates is $150 \mathrm{~N} / \mathrm{C}$. Calculate the final velcotiy of an electron as it leaves the plates.


## SPH4U 7.5 Electric Potential Due to Point Charges

## 1. Electric potential due to a point charge

| Electric field: |  |
| :--- | :--- |
| Electric potential due |  |
| to a point charge: |  |
| $\quad$sign |  |
| EE of two point <br> charges: |  |
| change in $E_{E}$ |  |

A point charge with a charge of $4.00 \times 10^{-8} \mathrm{C}$ is 4.00 m due west from a second
 point charge with a charge of $-1.00 \times 10^{-7} \mathrm{C}$.
a. Calculate the total electric potential due to these charges at a point $\mathrm{P}, 4.00 \mathrm{~m}$ due north of the first charge.
b. Calculate the work required to bring a third point charge with a charge of $2.0 \times 10^{-9}$ $C$ from infinity to point $P$.

A point charge $\mathrm{q}_{1}$ with charge $2.0 \times 10^{-6} \mathrm{C}$ is initially at rest at a distance of 0.25 m from a second charge $q_{2}$ with charge $8.0 \times 10^{-6} \mathrm{C}$ and mass $4.0 \times 10^{-9} \mathrm{~kg}$. Charge $\mathrm{q}_{1}$ remains fixed at the origin, whereas $q_{2}$ travels to the right upon release. Determine the speed of charge $q_{2}$ when it reaches a distance of 0.50 m from $\mathrm{q}_{1}$.

## 2. Head-on "collision"

Two particles, a proton with charge $1.60 \times 10^{-19} \mathrm{C}$ and mass $1.67 \times 10^{-27} \mathrm{~kg}$ and an alpha particle (He-4 nucleus) with charge $3.20 \times 10^{-19} \mathrm{C}$ and mass $6.64 \times 10^{-27} \mathrm{~kg}$, are separated by an extremely large distance. They approach each other along a straight line with initial speeds of $3.00 \times 10^{6} \mathrm{~m} / \mathrm{s}$ each. Calculate the separation between the particles when they are closest to each other.

## SPH4U 7.6 The Millikan Oil Drop Experiment

## 1. Millikan's experiment



Electric charge: excess protons

Calculate the charge on a small sphere with an excess of $3.2 \times 10^{14}$ electrons.

In a Millikan-type experiment, two horizontal plates aintained at a potential difference of 360 V are separated by 2.5 cm . A latex sphere with a mass of $1.41 \times 10^{-15} \mathrm{~kg}$ hangs between the plates, the upper plate of which is positive.
a. Is the sphere negatively or positively charged?
b. Calculate the magnitude of the charge on the latex sphere.
c. Determine the number of excess of deficit particles on the sphere.

## Quarks:

subatomic
particles

## SPH4U 8.1 Magnets and Electromagnets

## 5. Permanent magnets

| Magnetic field: |  |
| :---: | :--- |
| magnetic field <br> lines |  |
| magnetic poles |  |
| Earth's magnetic <br> field: |  |
| causes |  |
| compass |  |
| cosmic rays |  |



## 6. Electromagnetism

Principle of electromagnetism:
Right-hand rule for a
straight conductor:

## Right-Hand Rule for a Straight Conductor

If your right thumb is pointing in the direction of conventional current, and you curl your fingers forward, your curled fingers point in the direction of the magnetic field lines.



## Current loop:

## Solenoid:

Right-hand rule for a
solenoid:

## Right-Hand Rule for a Solenoid

If you coil the fingers of your right hand around a solenoid in the direction of the conventional current, your thumb points in the direction of the magnetic field lines in the centre of the coil.

## Electromagnet:

factors
applications

## SPH4U 8.2 Magnetic Force on Moving Charges

## 7. Magnetic force

```
Magnetic field
strength:
Magnetic force:
    equation
    direction
```


## Right-Hand Rule for a Moving Charge in a Magnetic Field

If you point your right thumb in the direction of the velocity of the charge $(\vec{V})$, and your straight fingers in the direction of the magnetic field $(\vec{B})$, then your palm will point in the direction of the resulting magnetic force $\left(\vec{F}_{\mathrm{M}}\right)$.

$\vec{B}$
The electron shown moves at a sped of $54 \mathrm{~m} / \mathrm{s}$ through a magnetic field with a strength of 1.2 T. The angle between the electron's velocity and the magnetic field is $90^{\circ}$. Assume the electron's charge is $-e=-1.60 \times 10^{-19} \mathrm{C}$.
a. What is the magnitude of the magnetic force on the electron?
b. Use the right-hand rule to determine the direction of the magnetic force.
c. Calculate the gravitational force on the electron $\left(m=9.11 \times 10^{-31} \mathrm{~kg}\right)$.
d. What is the ratio of gravitational force to magnetic force on the electron?

A proton is moving along the $x$-axis at a speed of $78 \mathrm{~m} / \mathrm{s}$. It enters a magnetic field of strength 2.7 T . The angle between the proton's velocity and the magnetic field is $38^{\circ}$. The mass of a proton is $1.67 \times 10^{-27} \mathrm{~kg}$.
a. Calculate the initial magnitude and direction of the magnetic force on the proton.

b. Determine the proton's initial acceleration.

During a thunderstorm, positive charge accumulates near the top of a cloud, and negative charge accumulates near the bottom. When the charge buildup is strong enough, negative charge moves rapidly from the cloud to the ground, as a lightning strike. Assume the charge is moving perpendicular to the ground, and Earth's magnetic field is horizontal, directed north. Determine the direction of the deflection of this charge by Earth's magnetic field.


## SPH4U 8.3 Magnetic Force on a Current-Carrying Conductor

## 8. Magnetic force and current

| Electric current: |  |
| :---: | :--- |
| single charge |  |
| wire with <br> current |  |
| direction |  |

A piece of wire 45.2 cm long has a current of 12 A . The wire moves through a uniform magnetic field with a strength of 0.30 T . Calculate the magnitude of the magnetic force on the wire when the angle between the magnetic field and the wire is:
a. $0^{\circ}$

b. $45^{\circ}$
c. $90^{\circ}$

Two electrical poles support a current-carrying wire. The mass of a 2.5 m segment of the wire is 0.44 kg , and a 15 A current travels through it. The convential current is due east, horizontal to Earth's surface. Earth's magnetic
 field is $57 \mu \mathrm{~T}$ and is oriented due north, horizontal to Earth's surface.
a. Determine the magnitude and direction of the magnetic force on the 2.5 m segment of wire.
b. Calculate the gravitational force on the 2.5 m segment of wire.

## 9. Applications

Loudspeakers:


## SPH4U 8.4 Motion of Charged Particles in Magnetic Fields

## 10. Uniform circular motion of charges

| Moving parallel to $\vec{B}:$ |  |
| :--- | :--- |
| Moving |  |
| perpendicular to $\vec{B}:$ |  |
| result |  |
| centripetal force |  |
| equation |  |

An electron ( $m=9.11 \times 10^{-31} \mathrm{~kg}$ ) starts from rest. A horizontally directed electric field accelerates the electron through a potential difference of 37 V . The electron then leaves the electric field and moves into a magnetic field with strength 0.26 T , directed into the page.

a. Determine the speed of the electron at the moment it enters the magnetic field.
b. Determine the magnitude and direction of the magnetic force on the electron.
c. Determine the radius of the electron's circular path.

## 11.Mass spectrometer

Mass
spectrometer:

A researcher using a mass spectrometer observes a particle travelling at $1.6 \times 10^{6} \mathrm{~m} / \mathrm{s}$ in a circular path of radius 8.2 cm . The spectrometer's magnetic field is perpendicular to the particle's path and has a magnitude of 0.41 T .
a. Calculate the mass-to-charge ratio of the particle.
b. Identify the particle using the table provided.

| Isotope | $\boldsymbol{m}(\mathrm{kg})$ | $\boldsymbol{q}(\mathbf{C})$ | $\frac{\boldsymbol{m}}{\boldsymbol{q}}(\mathbf{k g} / \mathbf{C})$ |
| :--- | :---: | :---: | :---: |
| hydrogen | $1.67 \times 10^{-27}$ | $1.60 \times 10^{-19}$ | $1.04 \times 10^{-8}$ |
| deuterium | $3.35 \times 10^{-27}$ | $1.60 \times 10^{-19}$ | $2.09 \times 10^{-8}$ |
| tritium | $5.01 \times 10^{-27}$ | $1.60 \times 10^{-19}$ | $3.13 \times 10^{-8}$ |

A researcher uses a mass spectrometer in a carbon dating experiment. The incoming ions are a mixture of ${ }^{12} \mathrm{C}^{+}$and ${ }^{14} \mathrm{C}^{+}$, and they have speed $v=1.0 \times 10^{5}$ $\mathrm{m} / \mathrm{s}$. The strength of the magnetic field is 0.10 T . The mass of an electron is 9.11 x $10^{-31} \mathrm{~kg}$, and the mass of protons and neutrons is $1.67 \times 10^{-27} \mathrm{~kg}$.

The researcher first positions the ion detector to determine the value of $r$ for ${ }^{12} \mathrm{C}^{+}$, then moves it to determine the value of $r$ for ${ }^{14} \mathrm{C}^{+}$. How far must the detector move between detecting the two isotopes?


